

Assignment 4

Due: Sunday, 13.05.2011, 23:59:59 via SVN

Task 1. *Complexity of append/3 (2 Points)*

For the following definition of `append/3`, show that it has linear complexity by showing that the depth of the derivation tree of any query to `append/3` has $n+1$ nodes, where n is the length of the list provided or constructed in the first argument:

```
append([X|Xs], Ys, [X|Zs]) :- append(Xs, Ys, Zs).
append([], Ys, Ys).
```

Task 2. *Shifting lists (2 Points)*

Implement a predicate “`shift(List1, List2)`” so that `List2` is `List1` ‘shifted rotationally’ by one element to the left. For instance,

```
?- shift([1,2,3,4,5], L2), shift(L2, L3).
```

should produce

```
L2 = [2,3,4,5,1]
L3 = [3,4,5,1,2]
```

Task 3. *Mapping list elements (4 Points)*

Implement a predicate “`translate(DigitList, WordList)`” that succeeds if `DigitList` is a list of digits and each element in `WordList` is the English word for the element at the same position of `DigitList`. For instance,

```
?- translate([1,2,3], L2).
```

should produce

```
L2 = [one, two, three]
```

and

```
?- translate(L1, [one, two, three]).
```

should produce

```
L1 = [1,2,3]
```

Tip: Start by considering how to represent the mapping of digits to words and vice versa. To check whether a term is a digit use the following helper predicate, which is itself based on a few built-in predicates that we haven't discussed yet but whose semantics should be obvious:

```
digit(X) :- number(X), X>=0, X<10.
```

Task 4. *Linear list* (4 Points)

Implement a predicate “linear(+NestedList, ?LinearList)” that succeeds whenever LinearList is a list whose elements may themselves be arbitrarily deeply nested lists and LinearList contains all elements of NestedList in the same order but without any nesting. For instance,

```
?-linear ( [1, [2, 3, [a, [b], c]]], L2 ).
```

should produce

```
L2 = [1, 2, 3, a, b, c]
```

Caution: Do not use any predefined predicates to implement your version of linear/2. Your solution must be self-contained.

Task 5. *List manipulation: Inserting elements* (5 Points)

a) (2 Points) Implement a predicate with the signature “insert_before(Elem, ElemNew, List, NewList)” that succeeds whenever NewList is the same as List but with ElemNew added before *each* occurrence of Elem. If Elem is not in List, the predicate should fail. For instance,

```
?- insert_before(c, b, [a, c, a, c, b, c], NewList).
```

should produce

```
NewList = [a, b, c, a, b, c, b, b, c]
```

- b) (2 Points) Document as precisely as possible in which invocation modes your insert_before/4 predicate is supposed to work and what it is doing in each case. Think in particular about deterministic and nondeterministic modes. Document only the most general modes that make a difference. For example, if a binary predicate p behaves the same for the modes p(+,+) and p(-,+) but differently for the mode p(-,-) and again differently for the mode p(+,-) then only document the behavior for p(+,+), p(-,-) and p(+,-).
- c) (1 Point) Demonstrate the consistency of your documentation and implementation by submitting traces of test queries that illustrate the behavior in each documented invocation mode. In the case of a '?' mode, illustrate the behavior for the '-' case.